

# A Survey of CBC MAC Variants

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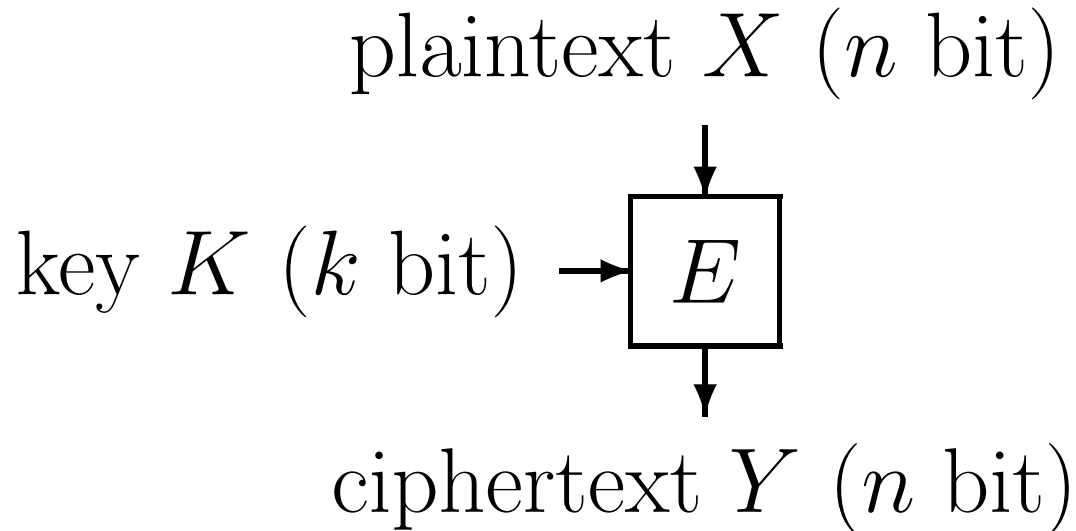
# CBC MAC Variants

EMAC, RMAC, XCBC, TMAC, OMAC.

Under consideration for standardization by NIST

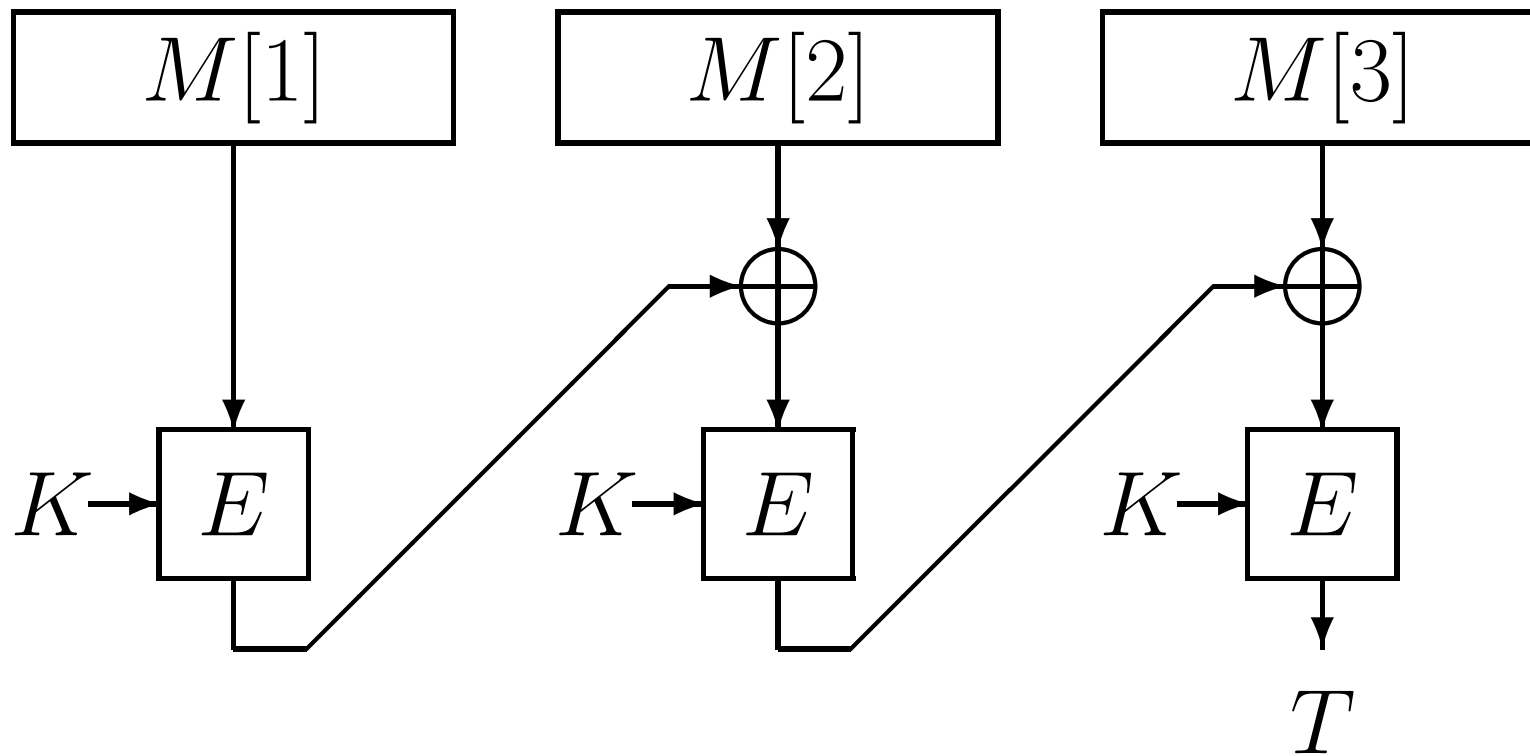
- Security
- Efficiency

**Block Cipher**  $E : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$



- Each  $E_K(\cdot)$  is a permutation on  $\{0, 1\}^n$ .
- Examples: AES, Camellia, TDES, ...

# CBC MAC



# CBC MAC

- Simple
- Secure (on messages of a **fixed** length) [BKR94]
- Widely standardized:

ANSI X9.19, FIPS 113, ISO 9797

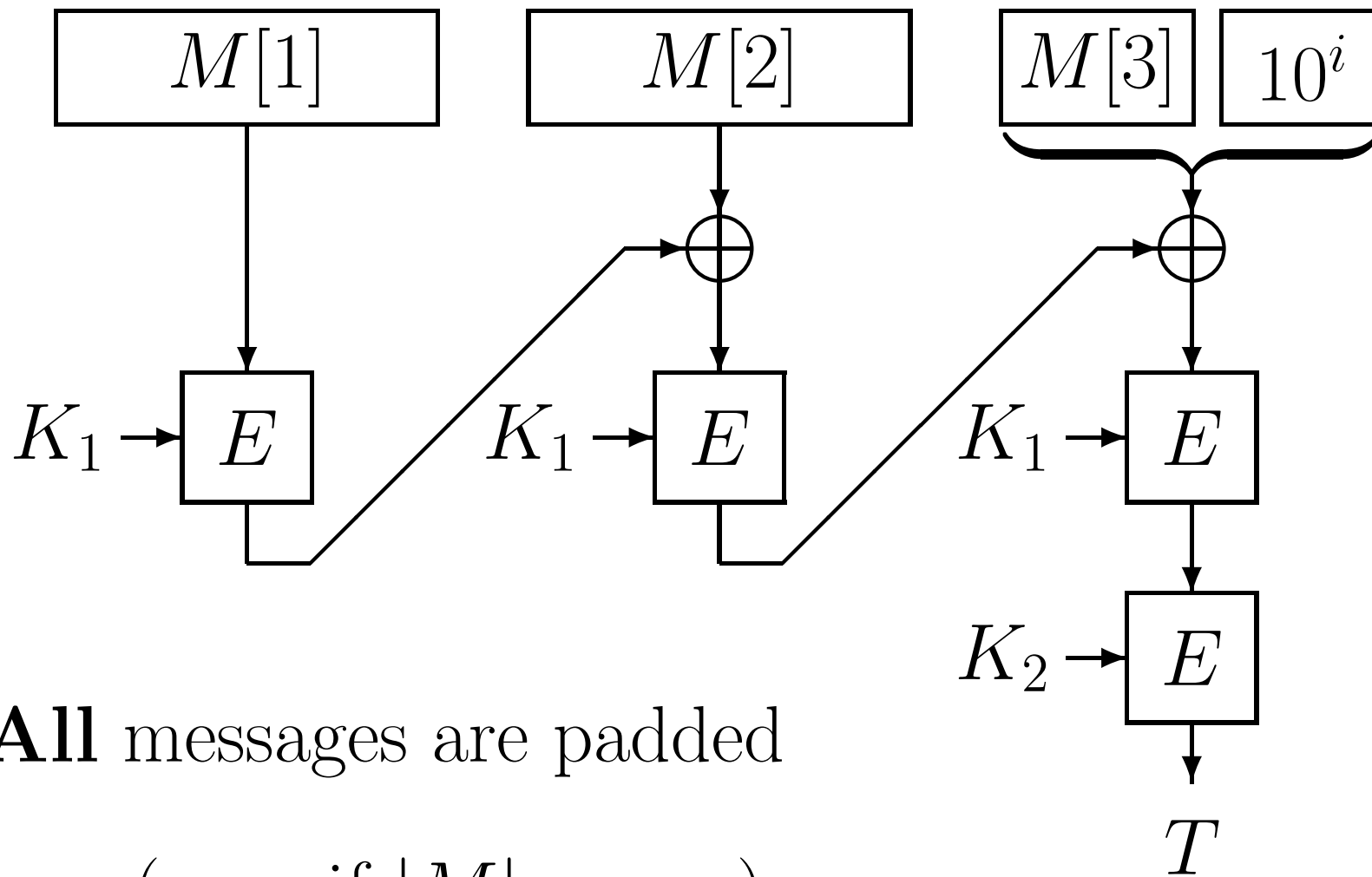
# Problems of CBC MAC

- does not allow messages of **varying** lengths  
(**insecure**)
- does not allow messages of **arbitrary bit length**  
(all messages must be a multiple of  $n$  bits)

# Proposals

- EMAC [Race Project, NESSIE]  
(Analysis by [Petrank, Rackoff])
- RMAC [Jaulmes, Joux, Valette]
- XCBC [Black, Rogaway]
- TMAC [Kurosawa, Iwata]
- OMAC [Iwata, Kurosawa]

# EMAC (Race Project, NESSIE)



**All** messages are padded  
(even if  $|M| = mn$ ).



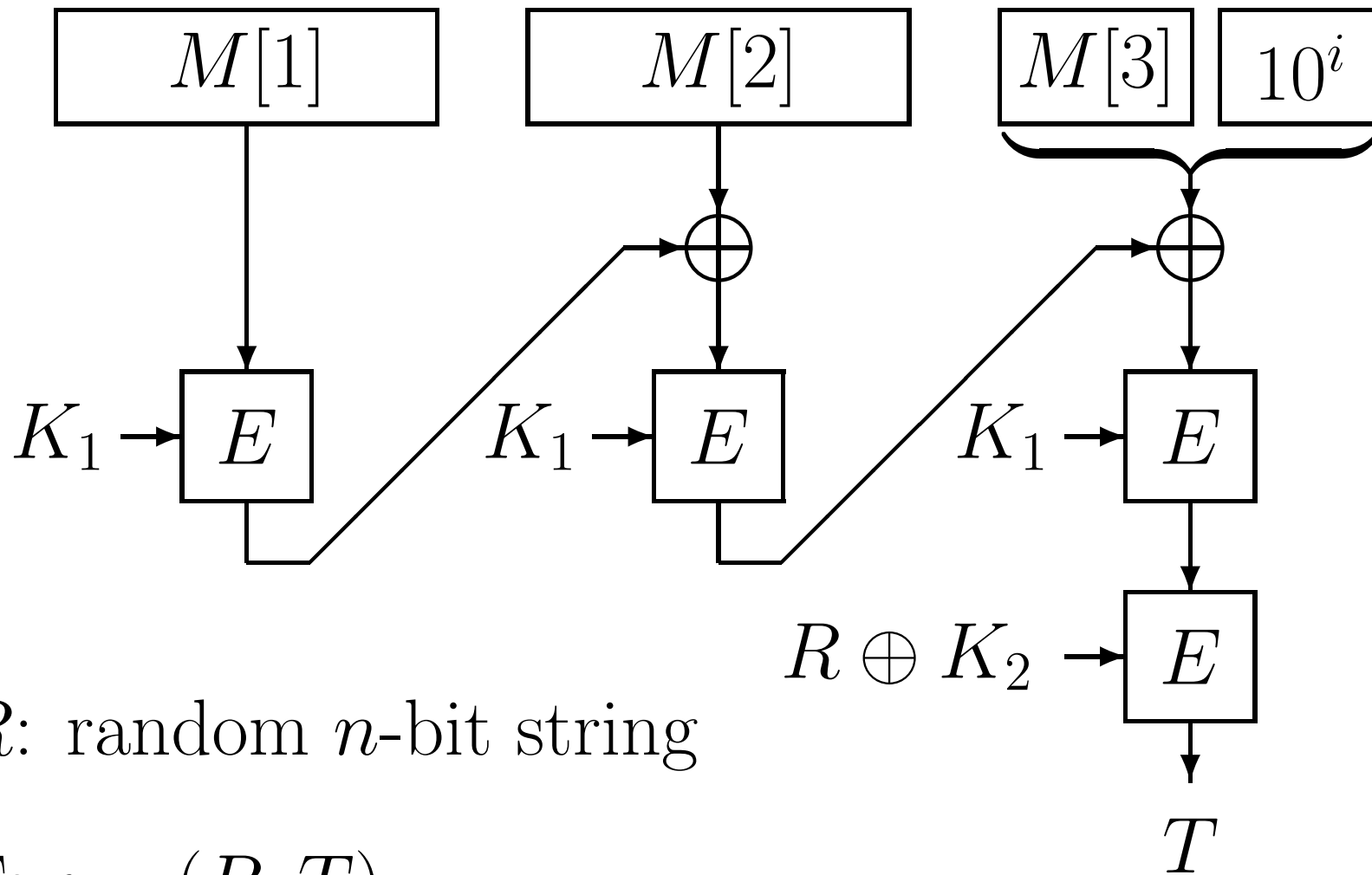
## Advantages of EMAC

- Secure for messages of varying lengths.  
(up to the birthday paradox limit)
- Allows messages of arbitrary bit length.

## Disadvantages of EMAC

- Needs two block cipher key schedulings.
- $m + 2$  block cipher invocations if  $|M| = mn$ .

# RMAC (JJV, FSE '02)



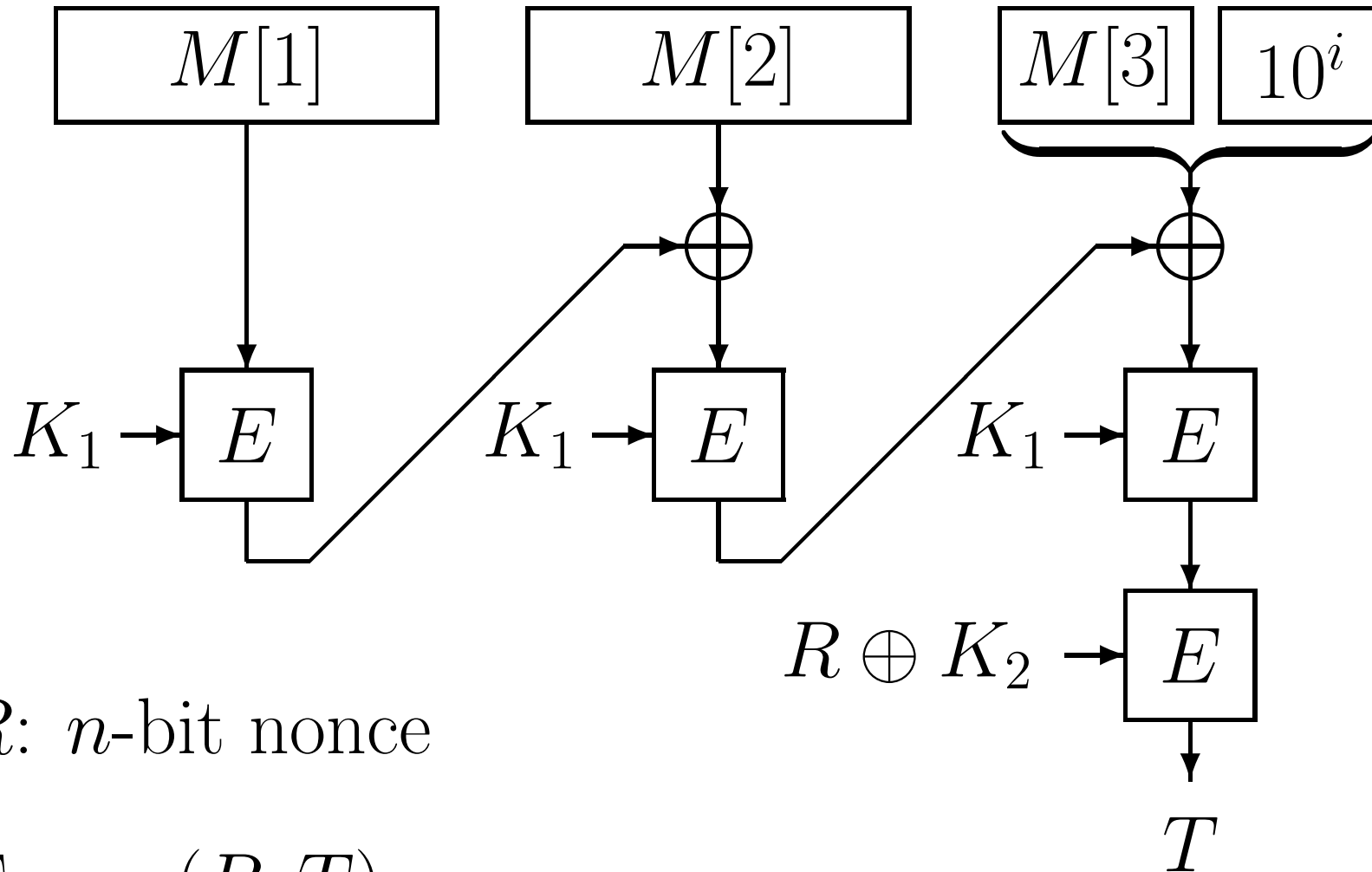
## Advantage of RMAC (JJV)

- Security beyond the birthday paradox limit.

## Disadvantages of RMAC (JJV)

- Security proof needs ideal block cipher.  
(No reduction based security)
- Inefficiency of EMAC.
- Needs random  $n$ -bit string for each  $M$ .

# RMAC (NIST '02)



$R$ :  $n$ -bit nonce

Tag =  $(R, T)$

## Advantage of RMAC (NIST)

- Reduction based proof.

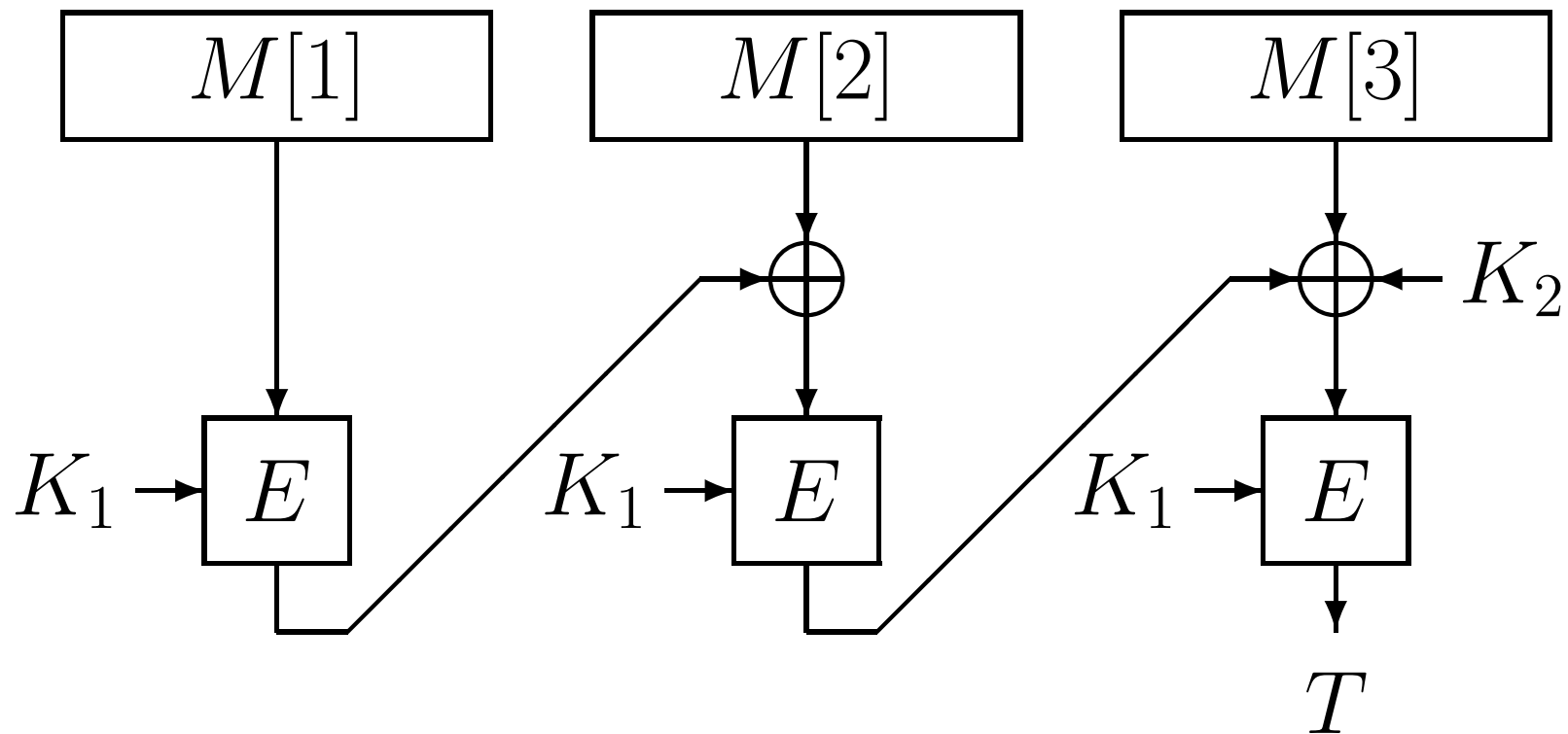
(up to the birthday paradox limit)

## Disadvantage of RMAC (NIST)

- Inefficiency of EMAC.

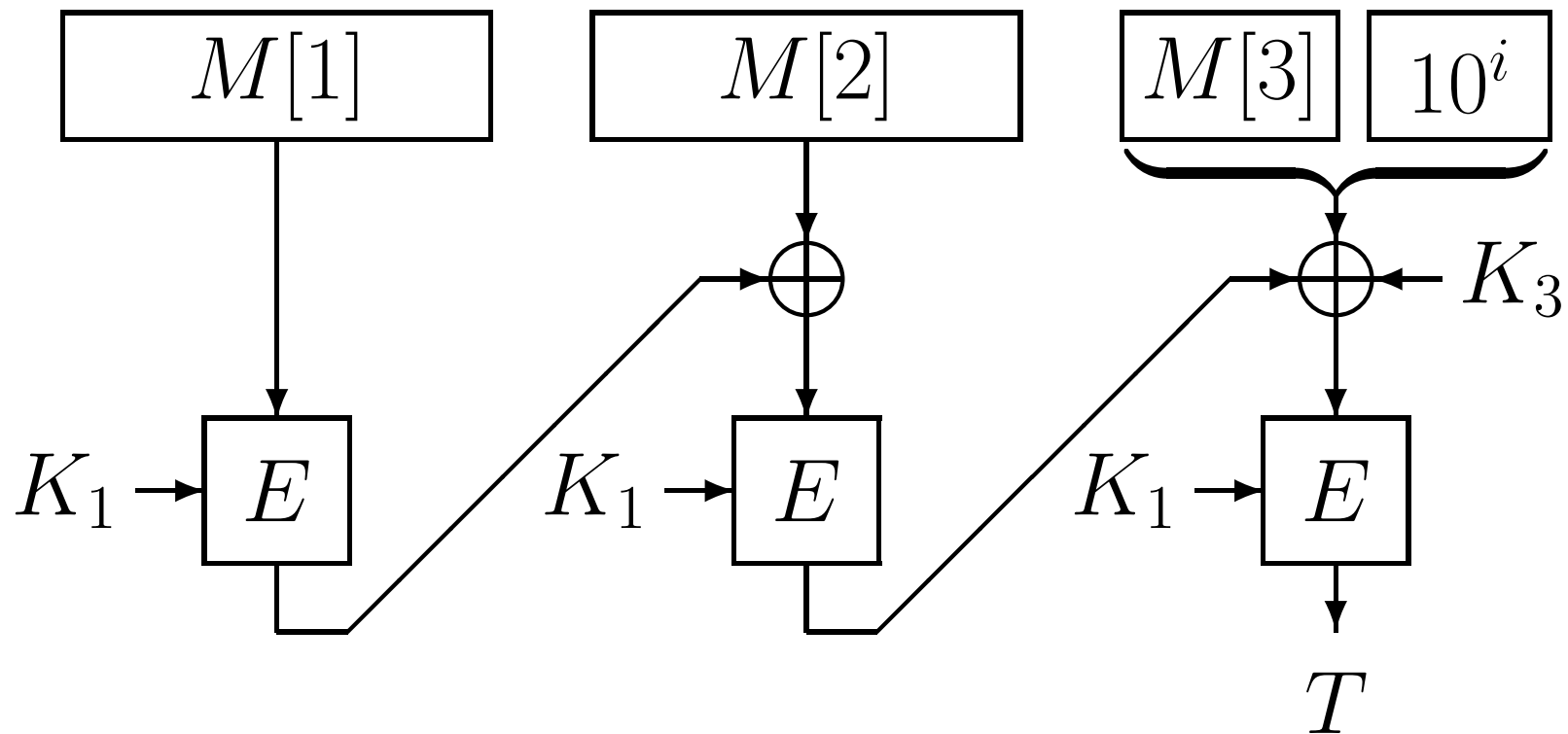
# XCBC (Black and Rogaway, Crypto'00)

Case  $|M| = mn$  ( $m \geq 1$ )



# XCBC (Black and Rogaway, Crypto'00)

Case  $|M| \neq mn$



## Advantages of XCBC

- 1 block cipher key scheduling.
- $\lceil |M|/n \rceil$  block cipher invocations.
- Same security as EMAC.

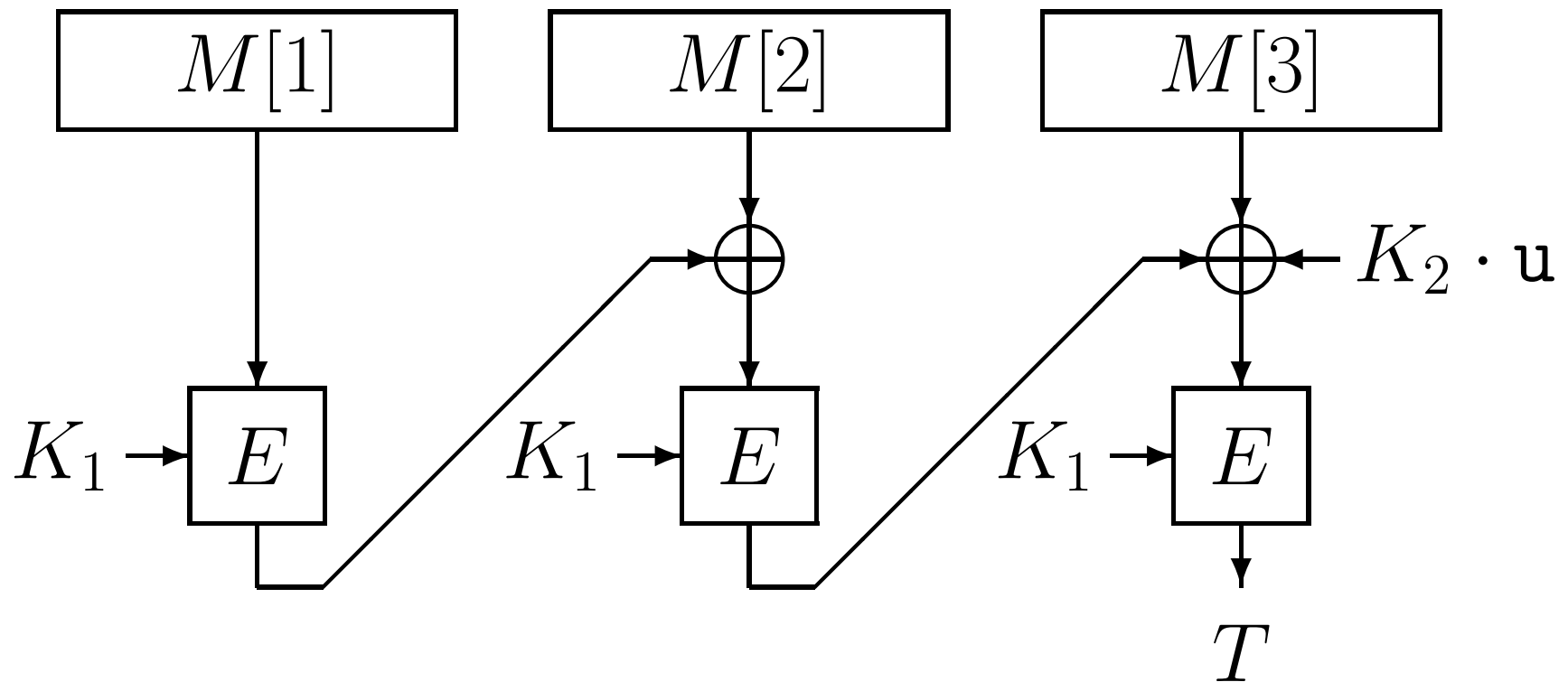
## Disadvantage of XCBC

- Three keys,  $K_1, K_2, K_3$ ,  $(k + 2n)$  bits in total.



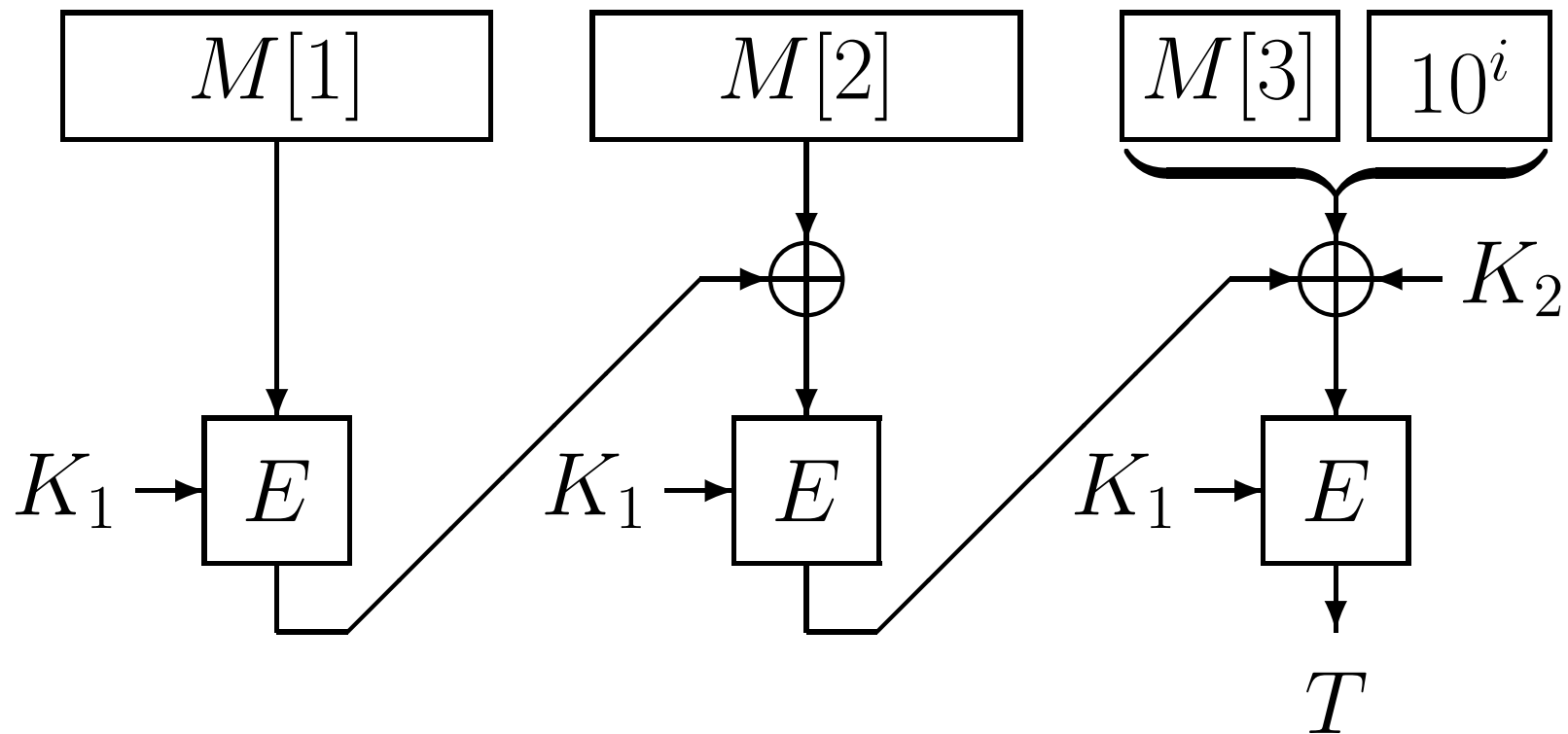
# TMAC (Kurosawa and Iwata, RSA '03)

Case  $|M| = mn$  ( $m \geq 1$ )



# TMAC (Kuroaswa and Iwata, RSA '03)

Case  $|M| \neq mn$



# Computation of $K_2 \cdot \mathbf{u}$ ( $\text{GF}(2^n)$ )

$$n = 128$$

$$a = a_{127}\mathbf{u}^{127} + \dots + a_1\mathbf{u} + a_0 = (a_{127}, \dots, a_1, a_0)$$

$$\mathbf{u} = (0, \dots, 0, 1, 0)$$

$$K_2 \cdot \mathbf{u} = \begin{cases} K_2 \ll 1 & \text{if } \text{msb}(K_2) = 0, \\ (K_2 \ll 1) \oplus \mathbf{Cst} & \text{otherwise.} \end{cases}$$

$$\mathbf{Cst} = 0^{120}10000111$$

## Advantages of TMAC

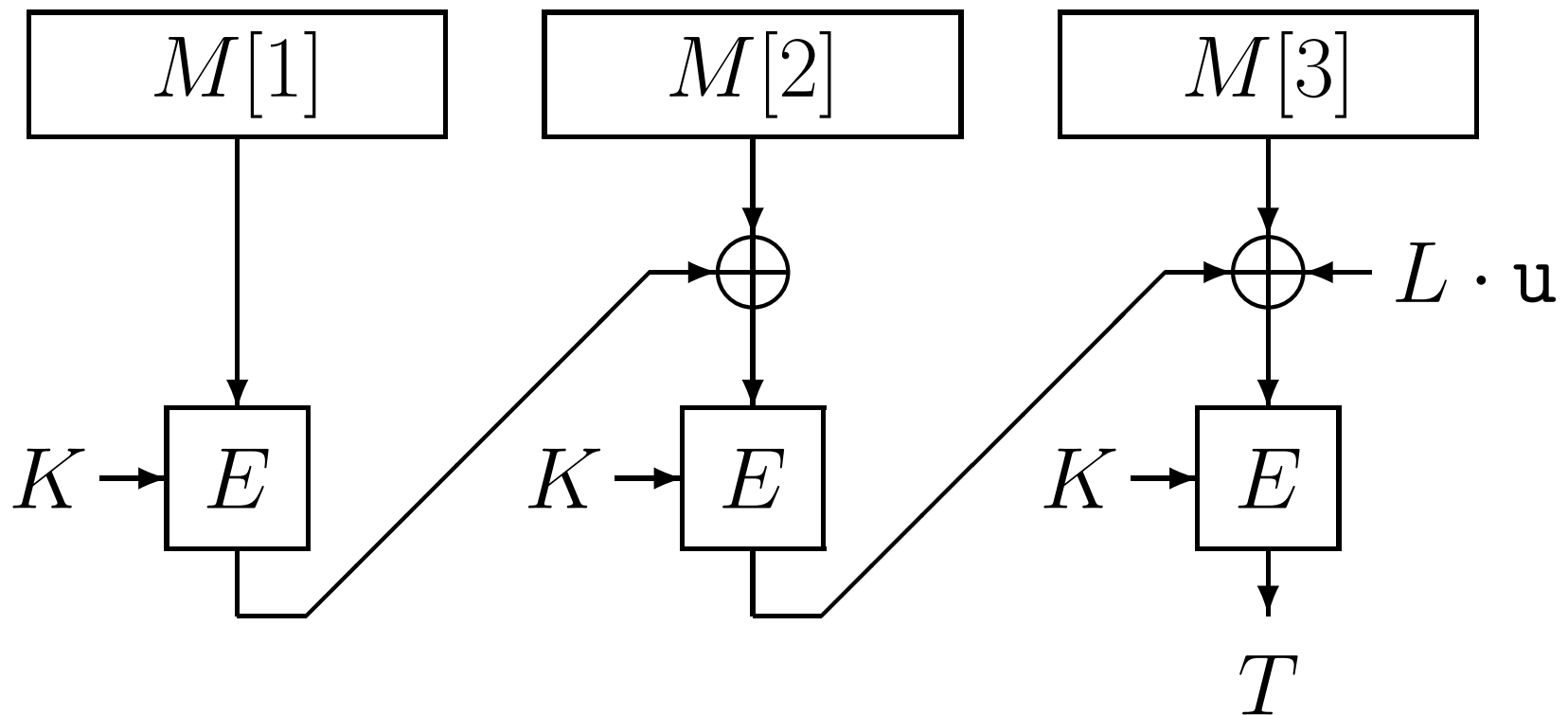
- Two keys,  $K_1, K_2$ ,  $(k + n)$  bits in total.
- No security loss.
- Negligible cost.

## Disadvantage of TMAC

- Two keys,  $K_1, K_2$ ,  $(k + n)$  bits in total.  
(longer than CBC MAC)

# OMAC1 (Iwata and Kurosawa, FSE '03)

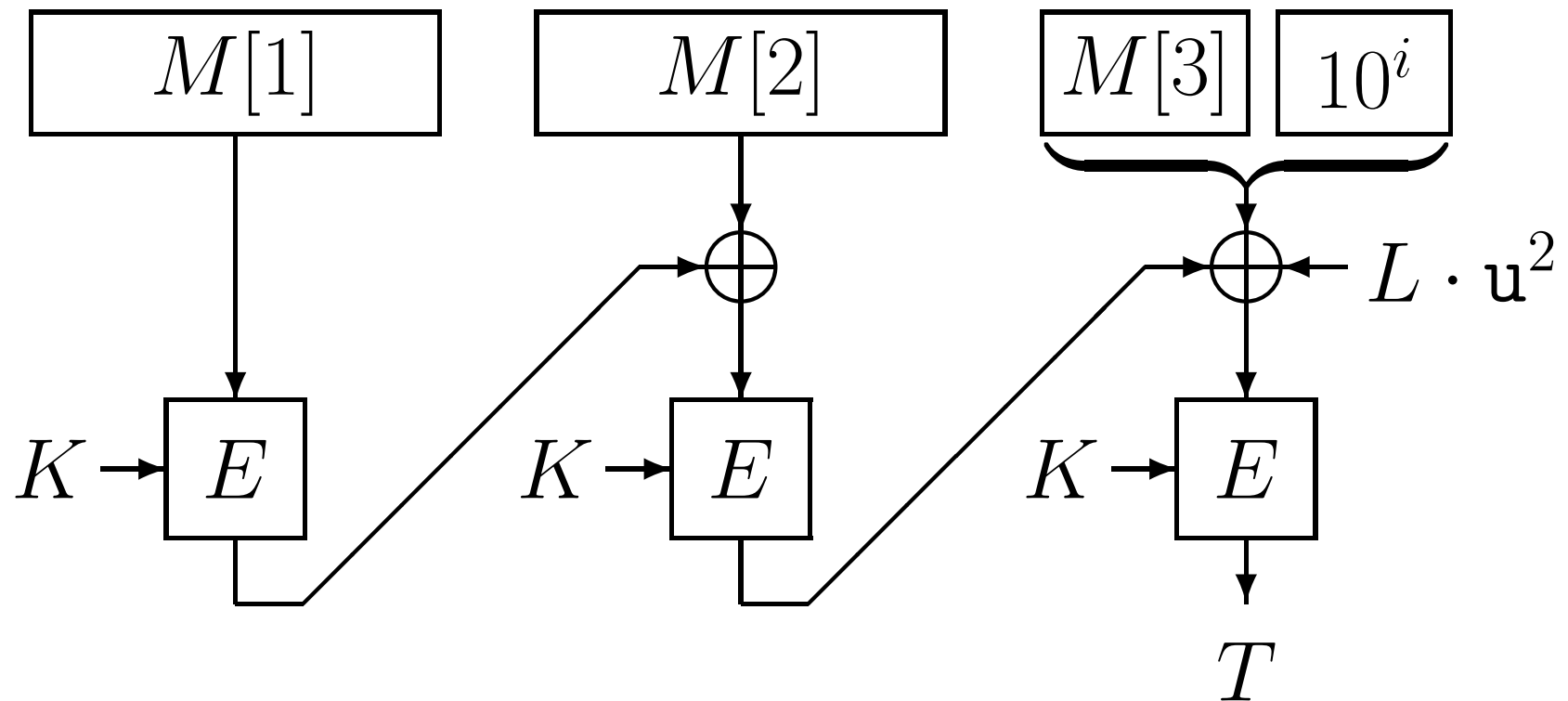
Case  $|M| = mn$  ( $m \geq 1$ )



$$L = E_K(0^n)$$

# OMAC1 (Iwata and Kurosawa, FSE '03)

Case  $|M| \neq mn$



$$L \cdot u^2 = (L \cdot u) \cdot u$$

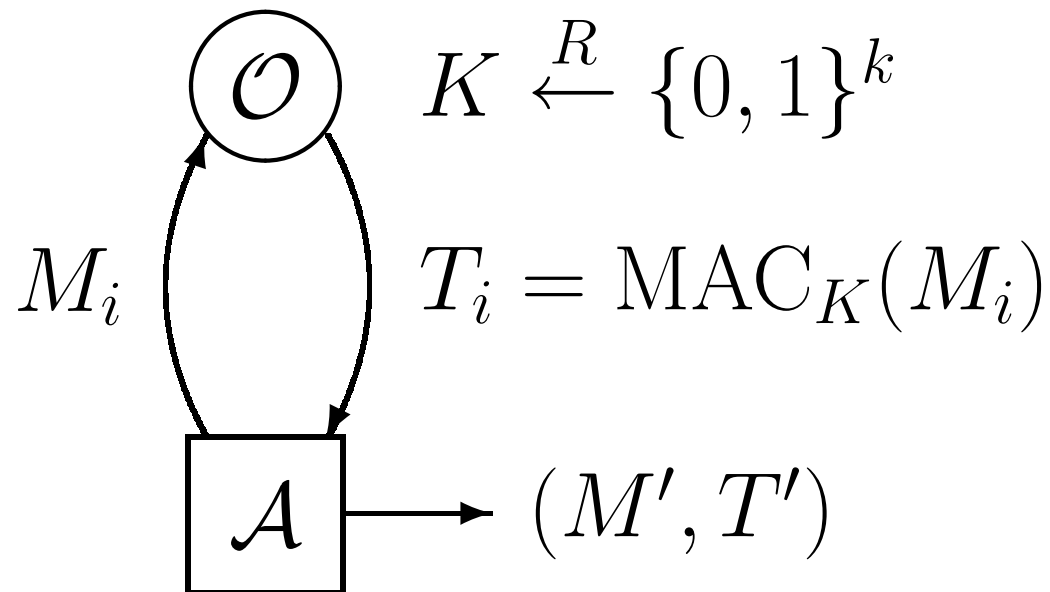
## Advantages of OMAC1

- One  $k$ -bit key  $K$ .
- No security loss.

## Disadvantage of OMAC1

- One block cipher invocation to compute  $L$ .

# Security of a MAC



- $\mathcal{A}$  forges if  $T' = \mathcal{O}(M')$ ,  $M' \neq M_i$
- $\text{Adv}_{\text{MAC}_K}^{\text{mac}}(\mathcal{A}) \stackrel{\text{def}}{=} \Pr_K(\mathcal{A} \text{ forges})$



## Security of a MAC (Cont.)

$$\text{Adv}_{\text{MAC}}^{\text{mac}}(q, \sigma) \stackrel{\text{def}}{=} \max_{\mathcal{A}} \left\{ \text{Adv}_{\text{MAC}}^{\text{mac}}(\mathcal{A}) \right\},$$

where  $\mathcal{A}$  asks at most  $q$  queries,

which are at most  $\sigma$  blocks in total.

- $\text{Adv}_{\text{EMAC}}^{\text{mac}}(q, \sigma) \leq \frac{3\sigma^2 + 1}{2^n} + \text{Adv}_E^{\text{prp}}(\sigma) + \text{Adv}_E^{\text{prp}}(q)$
- $\text{Adv}_{\text{RMAC(NIST)}}^{\text{mac}}(q, \sigma) \leq \frac{3\sigma^2 + 1}{2^n} + \text{Adv}_E^{\text{prp}}(\sigma) + \text{Adv}_{\Phi_k^\oplus, E}^{\text{prp-rka}}(q)$
- $\text{Adv}_{\text{XCBC}}^{\text{mac}}(q, \sigma) \leq \frac{3\sigma^2 + 1}{2^n} + \text{Adv}_E^{\text{prp}}(\sigma)$
- $\text{Adv}_{\text{TMAC}}^{\text{mac}}(q, \sigma) \leq \frac{3\sigma^2 + 1}{2^n} + \text{Adv}_E^{\text{prp}}(\sigma)$
- $\text{Adv}_{\text{OMAC}}^{\text{mac}}(q, \sigma) \leq \frac{4\sigma^2 + 1}{2^n} + \text{Adv}_E^{\text{prp}}(\sigma + 1)$

- $\text{Adv}_E^{\text{prp}}(q)$  is the maximum distinguishing probability between  $E$  and a random permutation,
- $\text{Adv}_{\Phi_k^\oplus, E}^{\text{prp-rka}}(q)$  is the maximum distinguishing probability between  $E$  and a family of random permutations (ideal block cipher) in the related key attack scenario (BK, Eurocrypt '03).
- The maximum is over all adversaries who make at most  $q$  queries.

# Discussion

Suppose that  $\text{Adv}_E^{\text{prp}}(\sigma)$  is small.

- EMAC, XCBC, TMAC and OMAC are secure.
- RMAC may not ( $\text{Adv}_{\Phi_k^\oplus, E}^{\text{prp-rka}}(q)$  may be large).

# Discussion

Suppose that TDES is used.

- $\text{Adv}_{\text{TDES}}^{\text{prp}}(\sigma)$  is small.
- $\text{Adv}_{\Phi_k^\oplus, \text{TDES}}^{\text{prp-rka}}(q)$  is small.

# Security Comparison

- $\text{EMAC} \approx \text{XCBC} \approx \text{TMAC} \approx \text{OMAC}$
- $\text{RMAC}$

# Efficiency Comparison

- $K$  len.  $\dots$  key length.
- $\#K$   $\dots$  Number of block cipher key schedulings.
- $\#E$  invo.  $\dots$  Number of block cipher invocations  
to compute a tag.
- $\#E$  pre.  $\dots$  Number of block cipher invocations  
in the pre-processing time.

# Efficiency Comparison

Name	$K$ len.	$\#K$	$\#E$ invo.	$\#E$ pre.
CBC	$k$	1	$ M /n$	0
EMAC	$2k$	2	$1 + \lceil ( M  + 1)/n \rceil$	0
RMAC	$2k$	$1 + \#M$	$1 + \lceil ( M  + 1)/n \rceil$	0
XCBC	$k + 2n$	1	$\lceil  M /n \rceil$	0
TMAC	$k + n$	1	$\lceil  M /n \rceil$	0
OMAC	$k$	1	$\lceil  M /n \rceil$	1



## OMAC needs one $E$ pre.

Not very significant:

- it can be done in an idle time.
- it is performed infrequently

(compared to MAC generation).

One or two  $E$  invo. in EMAC/RMAC is significant.

# Key Separation Technique (KST)

EMAC with TDES168.

$K$ : 168 bits  $\rightarrow K_1, K_2$ : 168 bits  $\times 2$

$$K_1 \stackrel{\text{def}}{=} \left\{ \begin{array}{l} \text{first 168 bits of} \\ \text{TDES}_K(\mathbf{C}_1) \circ \text{TDES}_K(\mathbf{C}_2) \circ \text{TDES}_K(\mathbf{C}_3) \end{array} \right.$$

$$K_2 \stackrel{\text{def}}{=} \left\{ \begin{array}{l} \text{first 168 bits of} \\ \text{TDES}_K(\mathbf{C}_4) \circ \text{TDES}_K(\mathbf{C}_5) \circ \text{TDES}_K(\mathbf{C}_6) \end{array} \right.$$

for some 64 bit constants  $\mathbf{C}_1, \dots, \mathbf{C}_6$

# Efficiency Comparison (TDES & KST)

Name	$K$ len.	$\#K$	$\#E$ invo.	$\#E$ pre.
EMAC	$k$	3	$1 + \lceil ( M  + 1)/n \rceil$	4 or 6
RMAC	$k$	$2 + \#M$	$1 + \lceil ( M  + 1)/n \rceil$	4 or 6
XCBC	$k$	2	$\lceil  M /n \rceil$	4 or 5
TMAC	$k$	2	$\lceil  M /n \rceil$	3 or 4
OMAC	$k$	1	$\lceil  M /n \rceil$	1

# Efficiency Comparison (AES & KST)

Name	$K$ len.	$\#K$	$\#E$ invo.	$\#E$ pre.
EMAC	$k$	3	$1 + \lceil ( M  + 1)/n \rceil$	2, 3 or 4
RMAC	$k$	$2 + \#M$	$1 + \lceil ( M  + 1)/n \rceil$	2, 3 or 4
XCBC	$k$	2	$\lceil  M /n \rceil$	3 or 4
TMAC	$k$	2	$\lceil  M /n \rceil$	2 or 3
OMAC	$k$	1	$\lceil  M /n \rceil$	1

## OMAC needs one $E$ pre.

The gain for this cost is its optimal key length, which *completely eliminates* the need for the KST.

- KST is a very error prone process in practice,
- Once KST is used, EMAC, RMAC, XCBC, TMAC have significant costs ( $\#K$ ,  $\#E$  pre.).

# Conclusion

Use OMAC!

- Good security bound.
- Good efficiency.

## Note

- OMAC paper is available at

<http://eprint.iacr.org/2002/180/>

- NIST's web page is

<http://csrc.nist.gov/encryption/modes/>

Questions?

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